



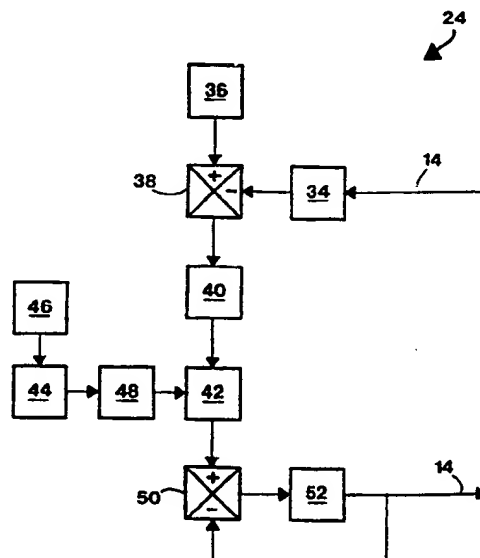
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(54) Title: ADAPTIVE CONTROL METHOD FOR MULTIEXCITER SINE TESTS

(57) Abstract

A multiexciter digitally swept-sinewave vibration test controller employing an adaptive control method which compensates for nonlinear and time variant physical characteristics of a system under test and for instrumentation errors. A system under test (12) is stimulated using an exciter array (26) and response is measured using a sensor array (28). The exciter array (26) is driven by signals produced by a digital vector swept oscillator (18). A control loop (14) is used to modify signals to the exciter array (26) based upon input from the sensor array (28). A digital processing system (24) processes signals in the control loop (14). Within the digital processing system (24), a system impedance matrix (44) containing values representing the inverse of response characteristics of the system under test (12) is updated to approximate an "actual" system impedance matrix. A drive signal matrix (52) is modified to cause the digital vector swept oscillator (18) to produce updated drive signals. An amount by which the updated system impedance matrix (44) is allowed to modify each iteration of the drive signal matrix (52) is controlled by a variable adjustment gain scalar (48). Value of the adjustment gain scalar (48) is determined using values obtained in a preceding iteration of the control cycle.



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ADAPTIVE CONTROL METHOD FOR MULTIEXCITER SINE TESTS**TECHNICAL FIELD**

The present invention relates generally to a method for correcting for nonlinearity in system characteristics during a vibration test, and more particularly to a method for accurately controlling stimuli applied by a multiexciter swept-sinewave control system so as to keep a resultant response matrix within acceptable limits. The predominant current usage of the adaptive control method for multiexciter swept sine tests of the present invention is in controlling the forces applied in the process of vibration stress analysis of engineered articles of manufacture.

BACKGROUND ART

Numerous factors have combined to create a need for increasingly accurate and repeatable stress and vibration testing of structures and devices. Among these are the trend to build things lighter and stronger, the increasing usage of new and untested materials, and an increasing awareness of the need for predictability and safety in the design and manufacture of products. Therefore, the field of vibration testing is rapidly advancing. Vibration testing is performed on actual items of manufacture where size and economy permit. Where this is not feasible, vibration testing may be performed on scale models or mock ups of items thought to have the same relative resistance to vibration as the actual items of interest.

U.S. Patent Nos. 3,710,082, and 3,848,115, both issued to Sloane et al., are concerned with the process of controlling essentially random signals with the objective of maintaining an overall spectral density of a vibration pattern within acceptable limits. Such an approach recognizes the random nature of many naturally occurring vibration sources. While this conceptual approach is perfectly valid and correct, it has been recognized that a more precisely defined stimulus might lead to a higher degree of repeatability in testing. One approach that has been

1 tried is to use motive stimulus defined by sine waves. Any
2 complex wave can be synthesized using a combination of sine
3 waves. Therefore, a multiexciter system with each exciter
4 being driven by precisely controlled sums of sine waves
5 could, theoretically, produce any desired complex vibration
6 pattern in a structure. In a multiexciter system, stimulus,
7 and response are best described by vectors of dimension N and
8 impedance factors are best described by a matrix of N by N
9 dimensions, with N being the number of stimulus/response
10 points involved.

11 The objective of a multiexciter swept-sinewave test is
12 to impart a controlled stimulus to a structure at specified
13 points via a series of actuators. A desired stimulus can be
14 represented as a complex vector spectrum. A multiexciter
15 controller, through feedback, continuously excites the
16 structure, measures the response spectral vector at the
17 control points, and modifies the drive signal spectral vector
18 until the response vector agrees with the desired stimulus
19 vector to within some acceptable error tolerance.

20 In the past, these tests have been performed using
21 purely analog means. In the analog systems, phase
22 relationships between response points were controlled by
23 inducing phase shifts between the drive signal components as
24 a function of the phase difference between the response
25 points. However, the analog approach proved to be largely
26 unsuccessful at frequencies near structural resonance
27 frequencies, since cross coupling effects between the drive
28 signal components and the structure's frequency response
29 characteristics were not accounted for.

30 More recently, digital approaches have been tried with
31 greater success. The most important reason for the success
32 of digital control systems in these applications is that
33 digital systems can employ a feedback control algorithm that
34 accounts for structural cross coupling effects by using a
35 structural frequency response matrix measured before the
36 test. U.S. Patent No. 4,782,324, issued to the present
37 inventor, teaches a method and apparatus for converting a
38 digital signal into an analog signal useful for vibration
39 exciter stimulation.

40 ///

1 However, even the currently available digital control
2 systems will not provide the desired degree of control when
3 applied to nonlinear and/or time varying systems because the
4 frequency response matrix estimate used by the control system
5 may differ from the actual frequency response matrix existing
6 during the test. For instance, nonlinear stiffness effects
7 will generally cause a shift in the resonant frequency that
8 will cause a large deviation in the phase of the measured
9 frequency response matrix as compared to the response matrix
10 which the control system actually encounters as it is
11 conducting the swept sine test. These potentially large
12 phase discrepancies can cause control system instabilities.
13 Further, imperfections in controller drive and response
14 circuits can lead to undetected inaccuracies in conventional
15 systems. Clearly, there is a need to be able to dynamically
16 compensate for nonlinear and time variant deviations in a
17 structure response matrix during vibration testing, and to
18 detect and correct for other system inaccuracies.

19 All of the prior art systems for digitally controlling
20 multiexciter swept-sinewave vibration testing within the
21 inventor's knowledge have employed a predetermined and set
22 structural frequency response matrix.

23 No prior art controller to the inventor's knowledge has
24 successfully compensated for non linear or time variant
25 factors in a system frequency response matrix. All
26 multiexciter swept-sinewave vibration test controllers to
27 date have suffered a high degree of inaccuracy or instability
28 when encountering such variable factors, especially near
29 structural resonance frequencies.

30

31 DISCLOSURE OF INVENTION

32

33 Accordingly, it is an object of the present invention
34 to provide a controller for multiexciter swept-sinewave
35 vibration testing which will produce a desired complex
36 stimulus vector spectrum at a full range of frequencies
37 including those near structural resonance.

38 It is another object of the present invention to
39 provide a controller for multiexciter swept-sinewave
40 vibration testing which will correct for instrumentation

1 errors, such as low matching of phase and amplitude between
2 driver input channels, low coherence between exciter drive
3 vector and control point response vector, and low dynamic
4 range of the input and output channels.

5 It is still another object of the present invention to
6 provide a means for dynamically adjusting a drive signal
7 spectral vector in a multiexciter swept-sinewave vibration
8 test to compensate for non linear and time variant
9 characteristics of the structure under test.

10 It is yet another object of the present invention to
11 provide a means to correct for factors in a multiexciter
12 swept-sinewave test control system which would tend to cause
13 a drive signal spectral vector to vary from a desired
14 stimulus spectral vector.

15 Briefly, the preferred embodiment of the present
16 invention is a digitally controlled multiexciter swept-
17 sinewave vibration test controller employing the inventive
18 method to refine an estimate of system impedance values
19 during the control process for causing a control point
20 response spectral vector to agree with a desired reference
21 spectral vector. As with previous swept-sinewave
22 controllers, the inventive controller functions by employing
23 a feedback control algorithm that accounts for structural
24 cross coupling effects in a structure under test by using a
25 structural frequency response matrix. However, the
26 controller of the present invention has the capability of
27 adjusting the structural frequency response matrix during
28 testing and then modifying drive signals accordingly.

29 System stability is insured by application of an
30 optimization process to the adaptive control process.

31 An advantage of the present invention is that test
32 reliability and repeatability are enhanced by improved
33 control of vibration stimuli.

34 A further advantage of the present invention is that
35 test integrity is maintained even at structural resonance and
36 anti-resonance frequencies of a structure under test.

37 Yet another advantage of the present invention is that
38 unacceptable instability is not introduced into a test by
39 time variant or nonlinear characteristics of a structure
40 under test.

1 Still another advantage of the present invention is
2 that inaccuracies and instability due to instrumentation
3 errors in a controller feedback system are effectively
4 reduced.

5 These and other objects and advantages of the present
6 invention will become clear to those skilled in the art in
7 view of the description of the best presently known modes of
8 carrying out the invention and the industrial applicability
9 of the preferred embodiments as described herein and as
10 illustrated in the several figures of the drawing.

11

12 BRIEF DESCRIPTION OF THE DRAWING

13

14 FIG. 1 is a block diagram of a swept-sinewave
15 controller employing the inventive method; and

16 FIG. 2 is a flow diagram showing digital signal
17 processing steps to implement the inventive method within a
18 digital signal processing system.

19

20 BEST MODE FOR CARRYING OUT INVENTION

21

22 The best presently known mode for carrying out the
23 invention is a multiexciter swept-sinewave vibration
24 controller suitable for implementing the inventive adaptive
25 control method. The predominant expected usage of the
26 inventive adaptive control method is in the design
27 experimentation and quality control phases of the production
28 of structural items and components of items which are
29 intended to withstand vibration forces. The inventive method
30 is particularly useful in the testing of relatively large or
31 complex structures which are capable of complex resonance or
32 of physical characteristics that vary with time, with
33 frequency, or with other test parameters.

34 The controller of the presently preferred embodiment of
35 the present invention is illustrated by means of a block
36 diagram in FIG. 1 and is designated therein by the general
37 reference character 10. Also shown in FIG. 1 is a system
38 under test 12 which, along with the controller 10 form
39 portions of a closed control loop 14. In many of its
40 substantial components and processes, the controller 10 does

1 not differ significantly from conventional multiexciter
2 swept-sinewave controllers. The physical structure is
3 similar to that of prior art controllers.

4 The conventional elements of the controller 10 include
5 a digital sweep oscillator 16, a digital vector swept
6 oscillator 18, a D/A subsystem 20, an A/D subsystem 22 and a
7 digital processing subsystem 24. Completing the closed
8 control loop 14 are an exciter array 26 and a sensor array
9 28. The exciter array 26 is made up of a quantity of
10 exciters 30 chosen by a user of the controller 10 to be the
11 most desirable for the system under test 12. The locations
12 of the exciters 30 on the system under test 12 are also
13 chosen by the user according to established principles which
14 form no part of the present invention. For illustrative
15 purposes, the control loop 14 is shown in FIG. 1 to include
16 three exciters 30. In this example of a configuration for
17 usage of the best presently known embodiment 10 of the
18 inventive controller, the sensor array 28 contains a quantity
19 of sensors 32 equal to the quantity of exciters 30, being
20 three in the present example. However, as will be discussed
21 hereinafter, the present invention may also be used with
22 "non-square" systems in which the quantities of exciters 30
23 and sensors 32 are not identical. The sensors 32 are placed
24 as close as possible to the exciters 30 so as to avoid, as
25 much as possible, error in the feedback loop 14 resulting
26 from dissimilarity between motion actually present at the
27 exciters 30 and that sensed at the sensors 32.

28 During testing, the digital vector swept oscillator 18
29 modifies a digital equivalent of a sine wave signal created
30 in the digital sweep oscillator 16 according to input derived
31 from the digital processing system 24. The D/A subsystem
32 converts the modified digital equivalent signal into an
33 analog signal suitable for driving the exciters 30. The
34 exciters 30 may be any of the commonly available linear or
35 rotary types of electromechanical exciter devices. The
36 present inventor's Patent No. 4,782,324 teaches a method and
37 apparatus for converting a digital signal into a band limited
38 analog signal which is used in the inventive controller 10.
39 When the exciters 30 have stimulated the system under test
40 12, the sensors 32 measure the resultant response. If there

1 were but one exciter 30 and one sensor 32, a response
2 measured at that one sensor 32 could rightly be considered to
3 be the effect of the stimulus imparted by the one exciter 30.
4 However, since in the present example three exciters 30 and
5 three sensors 30 are used, responses measured at the sensors
6 32 must be considered to be an N dimensional vector, with N
7 being the total number of exciter 30 and sensor 32 pairs.
8 Analog response signals created by the sensors 32 are
9 converted to digital equivalents by the A/D subsystem 22,
10 which digital input is provided to the digital processing
11 system 24.

12 Referring now to FIG. 2, wherein is shown a block flow
13 diagram of the digital signal processing flow which occurs
14 within the digital processing system 24, it can be seen that
15 the outputs of the A/D subsystem 22 are provided to the
16 digital processing system via the feed-back loop 14 and are
17 resolved into a control response vector 34. It should here
18 be noted that the enumerated features of FIG. 2 represent
19 analog equivalents of the digital manipulation that actually
20 occurs within the digital processing system 24. The notation
21 is customary for depicting analog equivalents of digital
22 signal processing steps. As one familiar with the art of
23 digital signal processing would appreciate, actual
24 mathematical functions may be performed in an order not
25 directly correlative to the analog equivalents depicted.
26 Transformation of the analog equivalent shown into the
27 digital signal processing actually performed is according to
28 well known practices and is not unique to the present
29 invention. The control response vector 34 is compared to a
30 reference spectrum vector 36 at a first comparator 38. A
31 control error vector 40 results from the first comparator 38.
32 Individual values of the control error vector 40 will be
33 positive where corresponding reference spectrum vector 36
34 values are higher than control response vector 34 values, and
35 negative where reference spectrum vector 36 values are lower
36 than control response vector 34 values. A compensated error
37 matrix 42 is produced by adjusting the control error vector
38 40 according to a system impedance matrix 44. The system
39 impedance matrix 44 is the set of inverse values of values
40 contained in a system response matrix 46. Initial values for

1 the system response matrix 46 are determined prior to
2 beginning a test by stimulating the system under test 12
3 sequentially with individual exciters 30 and measuring the
4 response of the system 12 at each sensor 32. An adjustment
5 gain scalar 48 is the factor by which the control error
6 vector 40 is adjusted by the system impedance matrix 44.
7 Means for adjusting the control error vector 40 by the system
8 impedance matrix 44 are well known and practiced in the art,
9 and are not unique to the present invention.

10 The compensated error matrix 42 is provided to a second
11 comparator 50. The second comparator 50 produces an updated
12 drive signal 52 which is provided as an output to the feed-
13 back loop 14. It is important to note that the operation
14 described above is both cyclical and continuous in nature,
15 and that the updated drive signal vector 52 being
16 instantaneously provided to the feedback loop 14 is also
17 provided as an input to the second comparator 50 such that
18 each succeeding cycle has as one component of the updated
19 drive signal vector 52 the updated drive signal vector 52 of
20 the previous cycle.

21 In mathematical terms the above described functioning
22 of the digital processing system 24 can be described as
23 follows:

24

25
$$\{D_{n+1}(f)\} = \{D_n(f)\} + g[Z_m(f)]\{R(f)\} - \{C_n(f)\}$$

26 where;

27 $D_n(f)$ = current values of the updated drive signal 52;

28 $D_{n+1}(f)$ = next subsequent values of the updated drive
29 signal 52;

30 g = value of the adjustment gain scalar 48;

31 $Z_m(f)$ = values of the system impedance matrix estimate
32 44;

33 $R(f)$ = values of the reference spectrum vector 36;

34 $C_n(f)$ = values of the control response vector 34; and

35 where the subscript "n" represents the number of the
36 current repetition and the subscript "m" represents the
37 fact that the associated quantities are measured and
38 determined prior to beginning the first test cycle.

39 ////

40 ////

1 It has been the practice in the industry to determine
2 the value of the adjustment gain scalar 48 at the outset of
3 the test to be a value "g" which is sufficiently large to
4 result in a reasonably quick system convergence, while
5 remaining small enough to reduce potential instability
6 problems caused by repeated excessive over correction of the
7 compensated error matrix 42 and, thus, of the updated drive
8 signal vector 52. Note that negative values of "g" have to
9 be used when phase errors greater than 90° are present in
10 measured values of the system response matrix 46. Further,
11 the values of the system response matrix 46 have also
12 heretofore been fixed during the test at values set prior to
13 the beginning of the test, as explained previously herein.

14 However, as is also explained previously herein, while
15 the digital processing system 24, as defined thus far, will
16 attempt to cause the control response vector 34 to converge
17 on the reference vector 36 values, it implicitly uses
18 assumptions that the system impedance matrix 44 is an
19 accurate measure of actual system characteristics under
20 dynamic test conditions. As discussed previously, this may
21 not be a good assumption, particularly over time as overall
22 system conditions, such as frequency and magnitude of input
23 stimuli, vary.

24 Therefore, in accordance with the method of the present
25 invention, a series of system response matrices 46 is
26 produced which converge to the inverse of an "actual" system
27 frequency response matrix "H(f)" (not shown). As will be
28 discussed hereinafter, an "actual" system response matrix,
29 because it may continually vary and because it is not
30 amenable to precise measurement, cannot be precisely defined,
31 and trying to define it is best viewed as a goal that can
32 never quite be achieved. Further, the presently preferred
33 embodiment of the present invention employs a variable
34 complex value for the adjustment gain scalar 48 which can
35 compensate for phase errors that can exist in updated system
36 response matrices 46 during early stages of the update
37 process, instead of the fixed value "g". The difficulty in
38 the process arises from the fact that any obvious approaches
39 to this require that the indefinable "actual" system response
40 matrix be known. The inventor has applied aspects of

1 optimization theory with aspects of control problem theory
 2 and an application of an algorithm that attempts to minimize
 3 an objective function to derive the unique process described
 4 herein which provides a means for accomplishing this
 5 seemingly impossible control dilemma.

6 According to the method of the present invention, the
 7 system impedance matrix 44 is updated according to the
 8 formula:

$$[Z_{n+1}(f)] = ([I_N] + \frac{([S_n(f)] - [Z_n(f)]([C_{n+1}(f)] - \{C_n(f)\}))([S_n(f)]^*)}{\langle [Z_n(f)]([C_{n+1}(f)] - \{C_n(f)\}), [S_n(f)] \rangle}) [Z_n(f)]$$

14 where:

15 $S_n(f)$ = values of the compensated error vector 40;

16 $Z_n(f)$ = values of the system impedance matrix 44;

17 $C_{n+1}(f)$ = next subsequent values of the control response
 18 vector 34;

19 $C_n(f)$ = present values of the control response vector 34;

20 $Z_n(f)$ = present values of the system impedance matrix 44;

21 $Z_{n+1}(f)$ = next subsequent values of the system impedance
 22 matrix 44;

23 I_N = the N dimensional identity matrix with N being the
 24 number of exciters 30 and sensors 32 in use.
 25
 26

27 It should be noted that, in accordance with the usage
 28 of the present invention, values of the compensated error
 29 vector 40 may properly also alternately be referred to as a
 30 vector "step" magnitude and direction because:
 31

$$[S_n(f)] = a_n[Z_n(f)]([R(f)] - \{C_n(f)\}) = [D_{n+1}(f)] - [D_n(f)]$$

32 where;

33 a_n = present value of the adjustment gain scalar 48.
 34
 35

36 In other words, the compensated error vector 40 is the
 37 amount by which values of the drive signal vector 52 are
 38 "stepped" between each cycle.

39 Values of the (variable) adjustment gain scalar 48 are
 40 determined by using a variation of a classic steepest decent

1 approach according to a formula and method described
2 hereinafter. The resulting value a_n is a steepest decent
3 complex gain value for the adjustment gain scalar 48.
4 Application of this method results in a change in control
5 error matrix 42 values between two successive control loop
6 iterations which are strictly non-negative. This means that
7 control error matrix 42 values will decrease even for
8 arbitrary invertible values of the system impedance matrix
9 44. This helps to assure that the controller 10 will be
10 stable. The use of a complex number for a_n is a refinement of
11 the previously mentioned technique of using negative values
12 of gain where phase deviation between values of the system
13 response matrix 46 exceeds 90° .

14 Furthermore, the vectors $\{S_n(f)\} = a_n[Z_n(f)]\{R(f)\} -$
15 $\{C_n(f)\}$ can be shown to be conjugate, since they are the
16 outcome of a steepest descent approximate Hessian algorithm.
17 Also, the impedance update, $[Z_{n+1}(f)]$ satisfies the secant
18 equation:

19

$$20 \quad [Z_{n+1}(f)](\{C_{n+1}(f)\} - \{C_n(f)\}) = \{S_n(f)\}$$

21

22 These two conditions guarantee (hypothetically) that
23 the system impedance matrix 44 will converge to the "actual"
24 impedance matrix within N steps, where N is the number of
25 independent exciters 30 that are being used to conduct the
26 test, if the underlying system being controlled is both
27 linear and time invariant.

28 The above described steps result in a method for
29 estimating the impedance of the system 12 during the control
30 process. The process is essentially stable and, converges in
31 at most N iterations for linear and time invariant systems
32 12. In the event the system under test 12 is nonlinear or
33 time variant, the method will track the impedance of the
34 system 12 as it varies with drive and control response
35 amplitudes and frequencies. Obviously, the controller 10
36 will not converge exactly in a finite number of steps.

37 The one remaining unresolved problem in the basic
38 scheme is that values of the complex quantity a_n depend upon
39 an unknown which is, generally, just as unknown as the
40 "actual" system response matrix $[H(f)]$. To solve this

dilemma, the inventor has employed a "two step control loop" wherein a "learning" loop is used to determine a value which is then used to calculate a_n , which is then used in a "control" loop. The "control" loop uses a_n to correct as much of any remaining error as is possible. The result of the "control" loop is then used to update impedance estimates followed by yet another "learning" loop. The cycle is repeated until the system 12 is brought under control.

To accomplish the "two step control loop" process, a variation of the classical multiexciter control update discussed previously is used:

12

13

$$\{D_n(f)\} = \{D_n(f)\} + c_n[Z_n(f)](\{R(f)\} - \{C_n(f)\})$$

15 where;

16

$\{D_n(f)\}$ = values of the drive signal vector 52 for the "learning" loop; and

c_n = value of the adjustment gain scalar 48 for the "learning" loop.

21

In the presently preferred embodiment of the invention, an initial value of approximately .1 is chosen for c_n in order to minimize control errors associated with using a possibly erroneous impedance estimate in the system impedance matrix 44. Values of c_n are allowed to increase as confidence in the accuracy of values within the system impedance matrix 44 is increased. Following the "learning" loop, the system under test 12 will respond with a "feedback" loop response value of the control response vector 34:

31

$$\{C_n(f)\}$$

From this, a value for the variable adjustment gain scalar 48 can be calculated as follows:

35

36

$$c_n < ((R(f) - \{C_n(f)\}), (\{C_n(f)\} - \{C_n(f)\})) >$$

38

39

40

$$a_n = \frac{\{C_n(f)\} - \{C_n(f)\}}{\|\{C_n(f)\} - \{C_n(f)\}\|^2}$$

1 As confidence in the values of the variable system
2 impedance matrix 44 increases, as measured by the value of
3 a_n , the value of c_n is allowed to approach 1.0. It should be
4 noted that an additional benefit can be derived from
5 monitoring the value of a_n . Since, as previously discussed,
6 values of the "actual" system response $[H(f)]$ cannot be known
7 exactly, it is useful to note that the value of a_n is the
8 best indicator of the instant reliability of the current
9 working values of the system response matrix $[Z_n(f)]$ 46.

10 The results described herein are relatively independent
11 of the initial value chosen for c_n and the rate at which it
12 is allowed to approach 1.0. However, obviously too small a
13 value for c_n will cause ill-conditioning of the a_n
14 calculation, and too large a c_n makes the controller 10 too
15 sensitive to system nonlinearities. Therefore, care in
16 choosing these values must still be exercised, and only some
17 minor experimentation with each different system will suffice
18 to try to optimize these values.

19 As described herein, a process for obtaining and using
20 all necessary values to achieve the described objectives can
21 be achieved by the interdependent steps of the inventive
22 process. All of the quantities required are available during
23 either the "learning" loop or the "control" loop. Use of the
24 inventive method does potentially increase control error
25 during initial iterations due to potential errors in initial
26 values assigned to the system response matrix 44. Careful
27 selection of values for c_n minimizes this problem.

28 Remaining problems to be addressed concerning the
29 present invention relate to sources of inaccuracy that are
30 inherent in any similar multiexciter sine wave type system.
31 Following is a discussion of how these problems are dealt
32 with in accordance with the best presently known embodiment
33 of the present invention.

34 The first such problem is low coherence between the
35 drive vector matrix 50 and the control point response vector
36 34. This low coherence results from noise in the measurement
37 of the control response vector 34 which is independent of
38 signals resulting from the drive vector 52. This sort of
39 error is corrected in the best presently known embodiment of
40 the present invention by employing a numeric algorithm to

1 synthesize a tracking filter in the digital domain in order
2 to measure the response at the fundamental frequency of the
3 drive signal. Algorithms for synthesizing analog filter
4 equivalents are well known and widely practiced in the
5 industry. This limits the effects of the contaminating
6 noise by reducing the bandwidth of the noise to match the
7 bandwidth of the tracking filter. Results of multiple
8 complex amplitude measurements are also averaged over several
9 repetitions to reduce the effects even further. However,
10 remaining noise still has an effect, and the greatest effect
11 will result near convergence of the system impedance matrix
12 44 to the "actual" system impedance.

13 A second such problem to be addressed is the effect of
14 poor matching between the several electrical channels leading
15 from the sensors 32. The mismatch is a result mainly of
16 differences between characteristics of low-pass filters that
17 are used ahead of the A/D converter channels in the A/D
18 subsystem 22 to prevent aliasing errors. The inventor has
19 found that this problem can be corrected by the same means
20 used with more conventional means of measuring frequency
21 response matrices. One solution is to use very high quality
22 components so as to match characteristics of all channels to
23 some acceptable level, such as $\pm .1$ dB in amplitude and ± 1.0
24 degree in phase. Another workable solution is to use a
25 software based calibration procedure, such as measuring the
26 frequency characteristics of the input subsystem and
27 correcting the input signal estimates thereby. Both methods
28 have been successfully employed with the present invention.
29 The best presently preferred embodiment uses the method of
30 employing high quality components. While this method is the
31 more costly, it has proven to be preferable.

32 A third such universal problem is that of low input and
33 output dynamic range. This causes noise to appear on both
34 the input vector 34 and on signals resulting from the output
35 vector 52. These problems are caused by finite resolutions
36 of the A/D subsystem 22 and D/A subsystem 20, or by low
37 efficiency transducers being used as exciters 30 or sensors
38 32. The problem is aggravated by the fact that significant
39 levels of signal component are produced at frequencies other
40 than the excitation frequency. Presence of these additional

1 signal components results in fundamental frequency response
2 being described by a small digital value in the A/D subsystem
3 20. The result is a larger percentage error in the control
4 response vector 34. The best solution to minimize this
5 problem has been found to be the use of high-resolution
6 components such as 16 bit converters in the A/D subsystem 22
7 and the D/A subsystem 20, and the use of full scale
8 excursions of high quality transducers consistent with analog
9 test levels.

10 By employing these several techniques in conjunction
11 with the inventive method for updating the system impedance
12 matrix 44 and for selecting appropriate variable values for
13 the adjustment gain scalar 44 during the test, the inventor
14 has found that the resulting controller 10 provides a
15 significant improvement over prior art vibration control
16 systems.

17 As discussed herein, the controller 10, according to
18 the present invention, effectively solves the problem of
19 inaccurate system impedance estimates caused by time variant
20 or non-linear system characteristics. It should be further
21 noted that the present invention provides an additional
22 benefit in that any synergistic effects caused by operating
23 multiple exciters 30 simultaneously, which could not be
24 accounted for using prior art technology, are not missed
25 using the inventive controller 10, since all measurements are
26 taken under actual operating conditions with all exciters 30
27 in operation. This last could prove to be one of the more
28 important advances in the field made by the present
29 invention.

30 As is shown above, in great part, the controllers 10
31 according to the present invention closely resemble prior art
32 conventional multiexciter swept-sinewave controllers in many
33 respects. The substantial difference exists in the inclusion
34 of means for updating impedance values and the use of a
35 complex variable gain factor for buffering modifications to
36 updated drive signals instead of a constant simple scalar
37 value. No significant changes of materials are envisioned
38 nor are any special constructions required.

39 Various modifications may be made to the invention
40 without altering its value or scope. For example, various

1 initial values of c_n can be tried to optimize the magnitude
2 of correction made on each repetitive step. Similarly, use
3 of lower or higher quality components or lower or higher
4 resolution digital components than are used in the best
5 presently known embodiment of the invention, as described
6 herein, would not change the basic character of the
7 invention.

8 Of course, the uniqueness of the invention, as
9 described herein, is not dependent upon use of any particular
10 quantity, type, or configuration of component parts.

11 Another conceivable change would be to vary the
12 sequence or nomenclature of quantities described by
13 mathematical formula herein, without essentially changing the
14 essence of the described invention.

15 As mentioned previously, while the best presently know
16 embodiment 10 of the invention has been described herein by
17 means of an example of use wherein an equal number of
18 exciters 30 and sensors 32 are employed, the invention
19 applies equally to "non-square" systems wherein the
20 quantities of exciters 30 differs from the quantity of
21 sensors 32 employed. Such a variation would require
22 considering an impedance matrix to be a N by M dimensional
23 matrix wherein N represents the quantity of exciters 30 and M
24 represents the quantity of sensors 32, and making
25 corresponding changes within the formulas given herein.

26 All of the above are only some of the examples of
27 available embodiments of the present invention. Those
28 skilled in the art will readily observe that numerous other
29 modifications and alterations may be made without departing
30 from the spirit and scope of the invention. Accordingly, the
31 above disclosure is not intended as limiting and the appended
32 claims are to be interpreted as encompassing the entire scope
33 of the invention.

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INDUSTRIAL APPLICABILITY

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37 The multiexciter swept-sinewave vibration test
38 controllers according to the present invention are
39 particularly adapted for controlling the vibrations applied
40 during vibration testing to structures having less than

1 perfectly stable structural impedance characteristics. The
2 predominant current usages are for testing the structural
3 integrity and resistance to vibration of structures
4 sufficiently large to be subject to significant complex
5 vibration patterns at or near an expected frequency of
6 induced vibration.

7 The multiexciter swept-sinewave vibration test
8 controllers of the present invention may be utilized in any
9 application wherein conventional multiexciter sine wave
10 controllers are used. The main area of improvement is in the
11 ability of the inventive controller to account for nonlinear
12 and time variant characteristics of the structure under test
13 such that instability and unreliable test results resulting
14 from such nonlinear and time variant characteristics are
15 avoided.

16 The control system 10 of the present invention affords
17 the additional advantage that it keeps a test structure's
18 response, at the fundamental frequency, relatively constant,
19 and thus minimizes both the effects of externally added noise
20 as well as the contribution of the finite resolution effects
21 of the A/D subsystem 22 and instrumentation effects.

22 Since the multiexciter digitally sept sine wave
23 vibration test controllers of the present invention may be
24 readily constructed and are physically significantly similar
25 to prior art conventional swept-sinewave controllers, it is
26 expected that they will be acceptable in the industry as
27 substitutes for the conventional controllers. Further, since
28 the controller of the present invention differs substantially
29 from many existing controllers primarily only in that minor
30 modifications cause the inventive controller to function
31 according to the inventive method, it is expected that many
32 existing controllers may be modified to function in
33 accordance with the present inventive method. For these and
34 other reasons, it is expected that the utility and industrial
35 applicability of the invention will be both significant in
36 scope and long-lasting in duration.

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In The Claims

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3 1. A method for controlling a plurality of analog sinewave
4 drive signals in a multiexciter vibration test, comprising
5 the steps of:

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a. stimulating a system under test with a
plurality of exciters, each of said exciters being a
transducer physically attached to an system under test,
for converting said analog sinewave drive signals into
mechanical motion;

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b. monitoring a response from said system under
test using a plurality of sensors, each of said sensors
being a transducer physically attached to said system
under test, for converting said response into an analog
response signal;

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c. converting said analog response signal into a
first digital signal;

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d. modifying said first digital signal as a
function of a reference spectrum vector and a measured
system response matrix, said reference spectrum vector
being a digital equivalent of a desired system motion,
said measured system response matrix being a digital
equivalent of a previously calculated system response,
such that an updated digital signal is produced which is
a digital equivalent of the analog sinewave drive
signals required to cause said first digital signal to
approach agreement with the reference spectrum vector;

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e. converting said updated digital signal into a
yet another plurality of analog sinewave drive signals
for again driving said exciters; and

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f. continuously repeating steps a. through e.
while updating values of said measured system response
matrix as a function of values obtained during previous
repetitions, such that a series of said measured system
response matrices is produced which are used in the
calculation of a series of said updated digital signals
for producing a series of said pluralities of said
analog sinewave drive signals, such that values for use
in calculating a next subsequent of said updated digital
signals are being obtained while each of said analog

- 1 sinewave drive signals is being used to excite the
2 system under test.
3
- 4 2. The method of Claim 1, wherein:
5 steps a. through e. are all accomplished in a less
6 time than a period of said analog sinewave drive
7 signals, such that each succeeding of said analog
8 sinewave drive signals is updated according to its
9 predecessor.
10
- 11 3. The method of Claim 1, and further including:
12 buffering effects of the measured system response
13 matrix according to a complex number gain value such
14 that, when said first digital signal is modified as a
15 function of the measured system response matrix, values
16 of said first digital signal are allowed to approach
17 values of the reference spectrum vector at a rate
18 determined as a function of a confidence value, said
19 confidence value being a function of a difference
20 between an instant set of values of said first digital
21 signal and a previous set of values of said first
22 digital signal.
23
- 24 4. The method of Claim 3, wherein:
25 said complex number gain value is determined as a
26 function of a trial gain value, the reference spectrum
27 vector, instant values of said first digital signal, and
28 previous values of said first digital signal.
29
- 30 5. The method of Claim 4, wherein:
31 said trial gain value is, itself, a function of
32 the instant values of said first digital signal and the
33 previous values of said first digital signal.
34
- 35 6. The method of Claim 1, wherein:
36 odd numbered repetitions of the method employ a
37 trial gain value for controlling an amount by which said
38 first digital signal is modified to produce said updated
39 drive signal, during which odd numbered repetitions of
40 the method updated values for said first digital signal

1 are obtained by digitizing the resultant analog response
2 signal, and also during which odd numbered repetitions
3 of the method the updated values for said first digital
4 signal are compared to previous values of said first
5 digital signal for determining an updated complex number
6 adjustment scale vector; and

7 even numbered repetitions of the method employ the
8 just determined updated complex number adjustment scale
9 vector for controlling an amount by which a previous
10 updated digital signal is modified by said first digital
11 signal and the measured system response matrix to
12 produce an instant updated digital signal, during which
13 even numbered repetitions of the method the trial gain
14 value is updated to reflect a confidence factor, said
15 confidence factor being a function of the amount by
16 which preceding iterations of said first digital signal
17 have varied.

18
19 7. In a method for controlling a cyclical sequence for
20 producing sets of sinewave drive signal digital equivalents
21 in a multiexciter sinewave vibration test controller, said
22 method including the steps of initially establishing a system
23 impedance matrix estimate and an adjustment gain scalar value
24 and further including the process of employing a feedback
25 control algorithm to account for a plurality of structural
26 cross coupling effects in a system under test by modifying a
27 control error vector according to said system impedance
28 matrix estimate, said control error vector being a difference
29 function between an input response vector and a desired
30 response vector and said system impedance matrix estimate
31 being a matrix of values representing said cross coupling
32 effects, an improvement for compensating for nonlinear and
33 time variant characteristics of the system under test
34 including the steps of:

35 a. stimulating the system under test using a
36 first set of the sinewave drive signals and measuring a
37 resultant physical response vector, the values of said
38 first set of sinewave drive signals having been
39 determined by modifying said control error vector
40 according to a first proportionate part of said system

1 impedance matrix estimate, said first proportionate part
2 being the product of said system impedance matrix
3 estimate multiplied by said adjustment gain scalar
4 value;

5 b. using the resultant input response vector to
6 calculate an appropriate value for a variable adjustment
7 gain complex number value and then stimulating the
8 system under test using a second set of sinewave drive
9 signals, said second set of sinewave drive signals
10 having been determined by modifying said control error
11 vector according to a second proportionate part of said
12 system impedance matrix estimate, said second
13 proportionate part being the product of said system
14 impedance matrix estimate multiplied by said variable
15 adjustment gain complex number value; and

16 c. repeating steps a. and b. such that during
17 each of alternate cycles of the method a new value for
18 said variable adjustment gain complex number is
19 obtained, and during each of those cycles during which
20 said variable adjustment gain complex number is not
21 being obtained, said variable adjustment gain complex
22 number is being used to determine said second
23 proportionate part of said system impedance matrix
24 estimate.

25

26 8. The improved method of Claim 7, wherein:

27 during alternate cycles of the method, the system
28 impedance matrix estimate is updated as a function of
29 the new value of said variable adjustment gain complex
30 number.

31

32 9. The improved method of Claim 7, wherein:

33 during alternate cycles of the method, the
34 adjustment gain scalar value is adjusted as a function
35 of a difference between prior values of said control
36 error vector.

37

38 10. The improved method of Claim 7, wherein:

39 a drive matrix, values of said drive matrix being
40 the sets of sinewave drive signal digital equivalents,

- 1 is updated during each cycle of the method by an amount
2 determined by a step value, said step value being the
3 control error vector modified by the system impedance
4 matrix estimate and the adjustment gain scalar value;
5 said step value is algebraically summed to a
6 present set of values of said drive matrix to determine
7 a next subsequent set of values of said drive matrix;
8 and
9 said system impedance matrix estimate is updated
10 on at least alternate cycles of said method according to
11 measured values of said control error vector.
12
- 13 11. The improved method of Claim 10, wherein:
14 the adjustment gain vector value is updated during
15 each cycle of the method as a function of a difference
16 between two prior values of the control error vector.
17
- 18 12. The improved method of Claim 7, wherein:
19 said system impedance matrix estimate is the set
20 of inverse values of digitized equivalents of the system
21 response matrix estimate, said system response matrix
22 estimate being calculated using data obtained during a
23 previous cycle of the method.
24
- 25 13. The improved method of Claim 7, wherein:
26 said adjustment gain scalar value is a complex
27 number, such that each value within the system impedance
28 matrix estimate will approach a corresponding value of
29 an actual system impedance matrix during each update of
30 the system impedance matrix estimate, said actual system
31 impedance matrix being an ideal matrix representing
32 instantaneous response characteristics of the system
33 under test.
34
- 35 14. The improved method of Claim 12, wherein:
36 values of the adjustment gain scalar are monitored
37 as an indicator of instant reliability of the system
38 impedance matrix estimate.
39
- 40 15. In a system for inducing controlled vibration patterns

1 in an article under test, said system including a plurality
2 of exciters physically attached to the article under test for
3 producing a physical motion in the article under test, a
4 plurality of sensors physically attached to the article under
5 test for sensing a resultant motion, an A/D subsystem for
6 converting analog sensor output into a digital output
7 equivalent of sensor output, a digital controller for
8 monitoring digital output from the A/D subsystem and for
9 producing a digital equivalent of a drive signal, and a D/A
10 subsystem for converting said digital equivalent of a drive
11 signal into an analog drive signal for powering the exciters,
12 said drive signal being a plurality of sinewaves with each of
13 said sinewaves being modified in phase and amplitude by the
14 digital controller such that said resultant motion tends to
15 conform to a predetermined desired motion, an improvement
16 comprising:

17 a first comparator means, logically situated first
18 within said digital controller such that said first
19 comparator means has as one of its inputs the digital
20 output from the A/D subsystem, for comparing a control
21 response vector to a reference spectrum vector and for
22 producing a control error vector as an output, said
23 control error vector representing the difference between
24 said control response vector and said reference spectrum
25 vector, said control response vector being a digital
26 equivalent of said resultant motion and said reference
27 spectrum vector being a digital equivalent of said
28 predetermined desired motion;

29 a buffering means, logically situated within said
30 digital controller after said first comparator means,
31 for modifying a system impedance matrix according to an
32 adjustment gain value and said control error vector and
33 for producing a compensated error matrix as an output,
34 said system impedance matrix containing inverse values
35 of a temporal system response matrix estimate, said
36 adjustment gain value being a value representing an
37 amount by which it is desired that said temporal system
38 response matrix estimate should be allowed to affect an
39 overall outcome, and said temporal system response
40 matrix being an estimate of an actual system response

1 matrix, said actual system response matrix representing
2 an ideal measurement of actual system response
3 characteristics which cannot actually be achieved; and

4 a second comparator means, logically situated
5 within said digital controller after said buffering
6 means, for comparing a current drive amplitude matrix
7 and said compensated error matrix and for producing an
8 updated drive amplitude matrix as an output, said
9 current drive amplitude matrix being a digital
10 equivalent of the plurality of sinewaves used for
11 powering the exciters, which current drive amplitude
12 matrix is returned to said second comparator by means of
13 a feed back loop functioning to return the current drive
14 amplitude matrix to the second comparator such that the
15 current drive amplitude matrix is an input to the second
16 comparator used in producing the updated drive amplitude
17 matrix, said compensated error matrix being the output
18 from the buffering means, and said updated drive
19 amplitude matrix serving to replace said current drive
20 amplitude matrix on a next subsequent cycle such that
21 the digital controller produces a continuing series of
22 updated drive amplitude matrices.
23

24 16. The improved system of Claim 15, wherein:
25 said adjustment gain value is a complex number.
26

27 17. The improved system of Claim 15, wherein:
28 said adjustment gain value is determined during a
29 learning loop, said learning loop being a cycle of
30 operation of the system wherein a learning loop gain
31 value is substituted for said adjustment gain value and
32 wherein system response to drive signal produced during
33 said learning loop is measured and used to calculate an
34 appropriate value for said adjustment gain value.
35

36 18. The improved system of Claim 17, wherein:
37 said learning loop gain value is initially
38 selected to be a real number less than 1.0.
39

40 19. The improved system of Claim 17, wherein:

1 said learning loop gain value is allowed to
2 approach a value of 1.0 as differences between
3 succeeding of the control response vectors becomes less.
4

5 20. The improved system of Claim 17, wherein:

6 each of said learning loops is followed by a
7 control loop, said control loop being a cycle of
8 operation of the system wherein said adjustment gain
9 value is used to buffer the system impedance matrix such
10 that the system impedance matrix is updated to approach
11 in value the actual system response matrix; and

12 each of said control loops is followed by a
13 learning loop at least until the system is under
14 control, as indicated by a value of said adjustment gain
15 value near unity.
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INTERNATIONAL SEARCH REPORT

International Application No **PCT/US90/02761**

I. CLASSIFICATION OF SUBJECT MATTER (If several classification symbols apply, indicate all) ¹ According to International Patent Classification (IPC) or to both National Classification and IPC IPC (5): G01M 7/00 US. CL.: 73/664		
II. FIELDS SEARCHED <div style="text-align: center; border-top: 1px solid black; border-bottom: 1px solid black; margin: 5px 0;">Minimum Documentation Searched ⁴</div> <div style="display: flex; justify-content: space-between; border-bottom: 1px solid black; margin: 5px 0;"> Classification System ¹ Classification Symbols </div> <div style="padding: 10px 0;"> U.S. : 73/664, 602; 364/508, 512; 340/683 </div> <div style="border-top: 1px solid black; padding: 10px 0; margin-top: 10px;"> Documentation Searched other than Minimum Documentation to the extent that such Documents are Included in the Fields Searched ⁵ </div>		
III. DOCUMENTS CONSIDERED TO BE RELEVANT ¹⁴		
Category ⁸	Citation of Document, ¹⁶ with indication, where appropriate, of the relevant passages ¹⁷	Relevant to Claim No. ¹⁸
A	US. A. 4,061,017 (SLOANE ET AL) 06 December 1977 See column 5, lines 5-37	1-20
A	US, A, 4,181,029 (TALBOTT, JR) 01 January 1980 See the abstract of the disclosure	1-20
A	US, A, 3,710,082 (SLOANE ET AL) 09 January 1973 See the abstract of the disclosure	1-20
<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>⁹ Special categories of cited documents: ¹³</p> <p>"A" document defining the general state of the art which is not considered to be of particular relevance</p> <p>"E" earlier document but published on or after the international filing date</p> <p>"L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)</p> <p>"O" document referring to an oral disclosure, use, exhibition or other means</p> <p>"P" document published prior to the international filing date but later than the priority date claimed</p> </div> <div style="width: 45%;"> <p>"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention</p> <p>"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step</p> <p>"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art.</p> <p>"&" document member of the same patent family</p> </div> </div>		
IV. CERTIFICATION		
Date of the Actual Completion of the International Search ² <div style="text-align: center; border: 1px solid black; padding: 5px; margin: 5px auto; width: 80%;">01 NOVEMBER 1990</div>	Date of Mailing of this International Search Report ³ <div style="text-align: center; border: 1px solid black; padding: 5px; margin: 5px auto; width: 80%;">13 FEB 1991</div>	
International Searching Authority ¹ <div style="text-align: center; border: 1px solid black; padding: 5px; margin: 5px auto; width: 80%;">ISA/US</div>	Signature of Authorized Officer ²⁰ <div style="text-align: center; margin-top: 10px;"> LOUIS M. ARANA </div>	

1/2

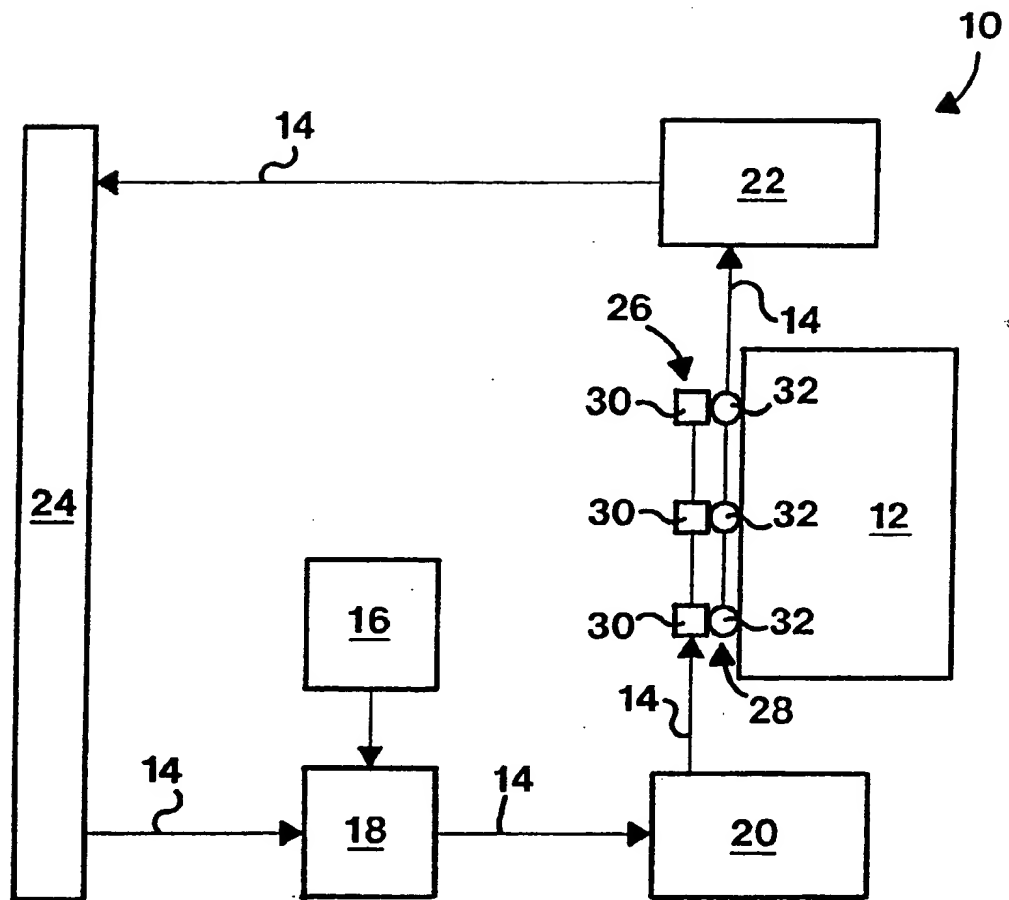


FIG. 1

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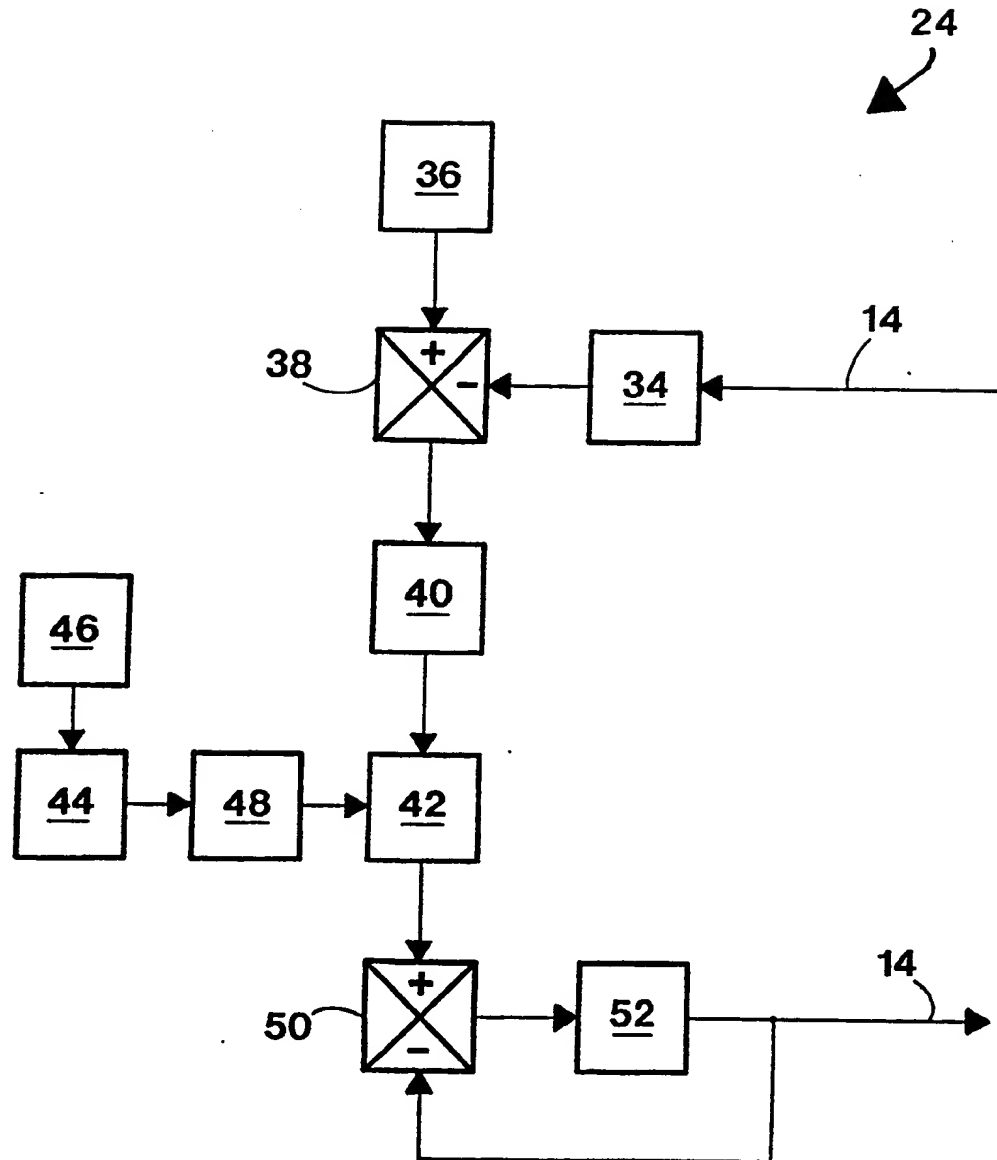


FIG. 2